New results on AdS black holes

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Based on

-1311.1795 (w/ A. Gnecchi, K. Hristov, C. Toldo, O. Vaughan) -1311.6937 (w/ S. Chimento) -1401.3107

Plan:

-Motivation: Why study AdS black holes?

-Noncompact horizons with finite volume

-Multi-centered solutions in AdS

-Final remarks

I) Why are AdS black holes interesting?

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 - AdS/cond-mat: quantum phase transitions, hologr.

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I) Why are AdS black holes interesting?
AdS/CFT (e.g. compare Euclidean AdS₄ gravity solutions with exact results in 3d superconformal field theories obtained by localization techniques)
AdS/cond-mat: quantum phase transitions, hologr. superconductors, ...

black holes in matter-coupled gauged sugra particularly interesting (bulk U(1) gauge field needed for finite density of charge carriers; considering bulk scalars means including scalar operators in the boundary dynamics)

- Holographic vitrification (Anninos, Anous, Denef, Peeters, 1309.0146): Black hole bound states in AdS are dual to structural glasses. Glassy feature of these multi-black holes related to their rugged free energy landscape, which is a consequence of the fact that constituents can have wide range of possible charges. - Holographic vitrification (Anninos, Anous, Denef, Peeters, 1309.0146): Black hole bound states in AdS are dual to structural glasses. Glassy feature of these multi-black holes related to their rugged free energy landscape, which is a consequence of the fact that constituents can have wide range of possible charges.

- Black hole entropy: Microscopic entropy counting for black holes in gauged supergravity? (4d AdS black holes are dual to 3d SCFTs. In the extremal case, the near-horizon geometry contains an AdS₂ factor, suggesting that the 3d SCFT flows to a superconformal quantum mechanics in the IR.)

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$$ds^{2} = -\frac{Q(q)}{p^{2} + q^{2}}(d\tau - p^{2}d\sigma)^{2} + \frac{P(p)}{p^{2} + q^{2}}(d\tau + q^{2}d\sigma)^{2} + (p^{2} + q^{2})\left(\frac{dq^{2}}{Q(q)} + \frac{dp^{2}}{P(p)}\right)$$
$$F = \frac{Q(p^{2} - q^{2}) + 2Ppq}{(p^{2} + q^{2})^{2}}dq \wedge (d\tau - p^{2}d\sigma) + \frac{P(p^{2} - q^{2}) - 2Qpq}{(p^{2} + q^{2})^{2}}dp \wedge (d\tau + q^{2}d\sigma),$$

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w/ the quartic structure functions

$$P(p) = \alpha - \mathsf{P}^2 + 2np - \varepsilon p^2 + (-\Lambda/3)p^4,$$

$$Q(q) = \alpha + \mathsf{Q}^2 - 2mq + \varepsilon q^2 + (-\Lambda/3)q^4.$$

P, Q : electric and magnetic charges. In what follows: P = 0 m, n : mass and NUT charge. Take n = 0 α and ε : additional non-dynamical parameters $\Lambda = -3/l^2$: Cosmological constant

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q radial coordinate, horizon at $q = q_h$, where $Q(q_h) = 0$ -Induced metric on horizon has correct signature iff $P(p) \ge 0$ -Since n = 0, P(p) has roots $\pm p_a$, $\pm p_b$, where $0 < p_a < p_b$ -Then $P(p) \ge 0$ for $|p| \le p_a$ or $|p| \ge p_b$. Consider range $|p| \le p_a$ (Range $|p| \ge p_b$ leads to different horizon topology)

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-Set
$$p = p_a \cos \theta$$
, $0 \le \theta \le \pi$

-Use scaling symmetry

$$p \to \lambda p$$
, $q \to \lambda q$, $\tau \to \tau/\lambda$, $\sigma \to \sigma/\lambda^3$,

 $\alpha \to \lambda^4 \alpha \,, \quad \mathbf{Q} \to \lambda^2 \mathbf{Q} \,, \quad m \to \lambda^3 m \,, \quad \varepsilon \to \lambda^2 \varepsilon \,,$

to set $p_b = l$ without loss of generality

-Define rotation parameter j by $p_a^2 = j^2$

Def. also
$$\tau =: t + \frac{j\phi}{\Xi}$$
, $\sigma =: \frac{\phi}{j\Xi}$, $\Xi := 1 - \frac{j^2}{l^2}$, $\Delta_{\theta} := 1 - \frac{j^2}{l^2} \cos^2\theta$

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+ some expression for the gauge pot. A \Rightarrow gives Kerr-Newman-AdS

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- Of course the solution above is singular in this limit
- \Rightarrow Have to study this case separately
- \Rightarrow Consider region $|p| \leq p_a$ and use scaling symmetry to set $p_a = l$

$$\Rightarrow P(p) = \frac{1}{l^2} (p^2 - l^2)^2$$

- Shift $\tau \to \tau + l^2 \sigma$ to avoid CTCs (we want σ to be compact coordinate)

$$ds_{\rm h}^2 = \frac{P(p)}{q_{\rm h}^2 + p^2} (q_{\rm h}^2 + l^2)^2 d\sigma^2 + \frac{q_{\rm h}^2 + p^2}{P(p)} dp^2$$

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Take limit $p \to l$ and define $\rho \equiv l - p$. Then:

$$ds_{\rm h}^2 \rightarrow (q_{\rm h}^2 + l^2) \left[\frac{d\rho^2}{4\rho^2} + 4\rho^2 d\sigma^2 \right] \Rightarrow \text{Hyperbolic space H}^2 !$$

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$$A_{\rm h} = \int (q_{\rm h}^2 + l^2) d\sigma dp = 2Ll(q_{\rm h}^2 + l^2) \qquad (\sigma \sim \sigma + L)$$

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- Thermodynamics: Compute M and J as Komar integrals associated to Killing vectors ∂_{τ} and $\partial_{\sigma} \Rightarrow$ Chirality-type condition $M = -J/l^2$

Tuesday, June 16, 15

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 - \Rightarrow First law should be

 $TdS = (1 - \Omega l^2)dL_0 + (1 + \Omega l^2)d\tilde{L}_0 - \phi_{\rm el}dQ$

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- ⇒ These exotic solutions may provide interesting new testgrounds to address questions related to black hole physics or holography

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These black holes violate reverse isoperimetric inequality

 \Rightarrow Superentropic black holes (1411.4309)

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Proposed Smarr formula for AdS black holes and associated extended version of first law that accounts for variations in the black hole mass w.r.t. variations in the cosmological constant

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(Note: Variable Λ goes back to Brown/Teitelboim 1987/1988 \Rightarrow 4d cosm. const. represents energy density of a 4-form gauge field strength. This idea was first applied to the thermodynamics of AdS black holes (KNAdS) in Caldarelli/Cognola/DK 9908022.)

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KRT: Obtained a general expression for the quantity $\Theta \equiv 8\pi G \frac{\partial M}{\partial \Lambda}$, that appears in both the first law and the Smarr formula, in terms of

surface integrals of the Killing potential $\omega \ (\xi^{\nu} = \nabla_{\mu} \omega^{\mu\nu})$

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(This is comparable to knowing that $\frac{\partial M}{\partial A} = \frac{\kappa}{8\pi G}$) \Rightarrow new term in first law of the form $\frac{\Theta}{8\pi G}\delta\Lambda$ (This is comparable to knowing that $\frac{\partial M}{\partial A} = \frac{\kappa}{8\pi G}$) \Rightarrow new term in first law of the form $\frac{\Theta}{8\pi G}\delta\Lambda$ Note: The cosmological constant can be thought of as a perfect fluid stress-energy w/ pressure $P = -\frac{\Lambda}{8\pi G}$ \Rightarrow suggests to interpret Θ as minus a *volume* \Rightarrow have $\frac{\Theta}{8\pi G}\delta\Lambda = V\delta P$ (This is comparable to knowing that $\frac{\partial M}{\partial A} = \frac{\kappa}{8\pi G}$) \Rightarrow new term in first law of the form $\frac{\Theta}{8\pi G}\delta\Lambda$ Note: The cosmological constant can be thought of as a perfect fluid stress-energy w/ pressure $P = -\frac{\Lambda}{8\pi G}$ \Rightarrow suggests to interpret Θ as minus a *volume* \Rightarrow have $\frac{\Theta}{8\pi G}\delta\Lambda = V\delta P$ Notice: The interpretation $\Theta = -V$ has an independent motivation: Express the surface integral for Θ as a volume integral using Gauss \Rightarrow One finds that $-\Theta$ gives a measure for the volume excluded from the spacetime by the black hole horizon (This is comparable to knowing that $\frac{\partial M}{\partial A} = \frac{\kappa}{8\pi G}$) \Rightarrow new term in first law of the form $\frac{\Theta}{8\pi G}\delta\Lambda$ Note: The cosmological constant can be thought of as a perfect fluid stress-energy w/ pressure $P = -\frac{\Lambda}{8\pi G}$ \Rightarrow suggests to interpret Θ as minus a volume \Rightarrow have $\frac{\Theta}{8\pi G}\delta\Lambda = V\delta P$ Notice: The interpretation $\Theta = -V$ has an independent motivation: Express the surface integral for Θ as a volume integral using Gauss \Rightarrow One finds that $-\Theta$ gives a measure for the volume excluded from the spacetime by the black hole horizon

For static black holes, the first law becomes $\delta M = T\delta S + V\delta P$, which is precisely the variation of the *enthalpy* H = E + PV

⇒ The mass of an AdS black hole should be thought of as the enthalpy of spacetime Cvetič/Gibbons/Kubizňak/Pope 1012.2888: Showed that $\left(\frac{(D-1)V}{\mathcal{A}_{D-2}}\right)^{\frac{1}{D-1}} \ge \left(\frac{A}{\mathcal{A}_{D-2}}\right)^{\frac{1}{D-2}}$ (1)

holds for a large class of black holes in AdS
Here: D = dimension of spacetime

A = horizon area
A_{D-2} = volume of unit S^{D-2}

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But...

The black holes that have noncompact horizon with finite area always violate the reverse isoperimetric inequality!

\Rightarrow 'Superentropic black holes'

(Hennigar/Mann/Kubizňak 1411.4309)

⇒ Suggests that reverse isoperimetric inequality conjecture might apply only to black holes w/ compact horizon

The proof of this restricted conjecture remains an interesting open problem

Start from charged generalization of McVittie solution (Reissner-Nordström immersed in FLRW, Shah/Vaidya 1968):

$$\begin{split} ds^{2} &= -\frac{\left[1 - (M^{2} - Q^{2})\frac{1 + kr^{2}}{4a^{2}r^{2}}\right]^{2}}{\left[1 + M\frac{\sqrt{1 + kr^{2}}}{ar} + (M^{2} - Q^{2})\frac{1 + kr^{2}}{4a^{2}r^{2}}\right]^{2}}dt^{2} \\ &+ 4a^{2}\left[1 + M\frac{\sqrt{1 + kr^{2}}}{ar} + (M^{2} - Q^{2})\frac{1 + kr^{2}}{4a^{2}r^{2}}\right]^{2}\frac{dr^{2} + r^{2}d\theta^{2} + r^{2}\sin^{2}\theta d\phi^{2}}{(1 + kr^{2})^{2}} \\ F &= \frac{Q}{ar^{2}}\frac{1}{\sqrt{1 + kr^{2}}}\frac{\left[1 - (M^{2} - Q^{2})\frac{1 + kr^{2}}{4a^{2}r^{2}}\right]}{\left[1 + M\frac{\sqrt{1 + kr^{2}}}{ar} + (M^{2} - Q^{2})\frac{1 + kr^{2}}{4a^{2}r^{2}}\right]^{2}}dr \wedge dt \,. \quad (a = a(t)) \end{split}$$

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$$F = \frac{Q}{ar^{2}}\frac{1}{\sqrt{1+kr^{2}}}\frac{\left[1 - (M^{2} - Q^{2})\frac{1+kr^{2}}{4a^{2}r^{2}}\right]}{\left[1 + M\frac{\sqrt{1+kr^{2}}}{ar} + (M^{2} - Q^{2})\frac{1+kr^{2}}{4a^{2}r^{2}}\right]^{2}}dr \wedge dt. \quad (a = a(t))$$

M = Q = 0: FLRW universe a = const., k = 0: Reissner-Nordström (in isotropic coordinates)

Start from charged generalization of McVittie solution (Reissner-Nordström immersed in FLRW, Shah/Vaidya 1968):

$$ds^{2} = -\frac{\left[1 - (M^{2} - Q^{2})\frac{1+kr^{2}}{4a^{2}r^{2}}\right]^{2}}{\left[1 + M\frac{\sqrt{1+kr^{2}}}{ar} + (M^{2} - Q^{2})\frac{1+kr^{2}}{4a^{2}r^{2}}\right]^{2}}dt^{2} + 4a^{2}\left[1 + M\frac{\sqrt{1+kr^{2}}}{ar} + (M^{2} - Q^{2})\frac{1+kr^{2}}{4a^{2}r^{2}}\right]^{2}\frac{dr^{2} + r^{2}d\theta^{2} + r^{2}\sin^{2}\theta d\phi^{2}}{(1+kr^{2})^{2}} F = \frac{Q}{ar^{2}}\frac{1}{\sqrt{1+kr^{2}}}\frac{\left[1 - (M^{2} - Q^{2})\frac{1+kr^{2}}{4a^{2}r^{2}}\right]}{\left[1 + M\frac{\sqrt{1+kr^{2}}}{ar} + (M^{2} - Q^{2})\frac{1+kr^{2}}{4a^{2}r^{2}}\right]^{2}}dr \wedge dt . \quad (a = a(t))$$

M = Q = 0: FLRW universe a = const., k = 0: Reissner-Nordström (in isotropic coordinates) - Solves Einstein-Maxwell equations

$$G_{\mu\nu} = 8\pi T_{\mu\nu} , \qquad \nabla_{\nu} F^{\mu\nu} = 4\pi J^{\mu}$$

where

$$T_{\mu\nu} = \frac{1}{4\pi} \left[F_{\mu\rho} F_{\nu}{}^{\rho} - \frac{1}{4} g_{\mu\nu} F_{\rho\lambda} F^{\rho\lambda} \right] + \rho u_{\mu} u_{\nu} + p(u_{\mu} u_{\nu} + g_{\mu\nu}),$$

(Maxwell + perfect fluid)

 $J^{\mu} = \sigma u^{\mu}$

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- Pressure, energy density, charge density and 4-velocity of fluid:

$$(\ddot{a} - \dot{a}^2) \left[1 + M \frac{\sqrt{1+kr^2}}{4} + (M^2 - Q^2) \frac{1+kr^2}{4} \right] = \dot{a}^2$$

$$8\pi p = -2\left(\frac{\ddot{a}}{a} - \frac{\dot{a}^2}{a^2}\right) \frac{\left[1 + M\frac{\sqrt{1+kr^2}}{ar} + (M^2 - Q^2)\frac{1+kr^2}{4a^2r^2}\right]}{\left[1 - (M^2 - Q^2)\frac{1+kr^2}{4a^2r^2}\right]} - 3\frac{\dot{a}^2}{a^2} - k\left\{a^2\left[1 + M\frac{\sqrt{1+kr^2}}{ar} + (M^2 - Q^2)\frac{1+kr^2}{4a^2r^2}\right]^2\left[1 - (M^2 - Q^2)\frac{1+kr^2}{4a^2r^2}\right]\right\}^{-1}$$

$$\begin{split} &8\pi\rho =& 3\frac{\dot{a}^2}{a^2} + \frac{3k}{2a^2} \left[1 + M\frac{\sqrt{1+kr^2}}{a\,r} + (M^2 - Q^2)\frac{1+kr^2}{4\,a^2\,r^2} \right]^{-3} \left[2 + M\frac{\sqrt{1+kr^2}}{a\,r} \right] \,, \\ &4\pi\sigma = -\frac{3}{4}\frac{kQ}{a^3}\frac{\sqrt{1+kr^2}}{r} \left[1 + M\frac{\sqrt{1+kr^2}}{a\,r} + (M^2 - Q^2)\frac{1+kr^2}{4\,a^2\,r^2} \right]^{-3} \,, \\ &u = \frac{1 - (M^2 - Q^2)\frac{1+kr^2}{4\,a^2\,r^2}}{1 + M\frac{\sqrt{1+kr^2}}{a\,r} + (M^2 - Q^2)\frac{1+kr^2}{4\,a^2\,r^2}} dt \,. \end{split}$$

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$$-k\left\{a^{2}\left[1+M\frac{\sqrt{1+kr^{2}}}{a\,r}+(M^{2}-Q^{2})\frac{1+kr^{2}}{4\,a^{2}\,r^{2}}\right]^{2}\left[1-(M^{2}-Q^{2})\frac{1+kr^{2}}{4\,a^{2}\,r^{2}}\right]\right\}^{-1},$$

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- Note also: p, ρ, σ are inhomogeneous (pressure gradient prevents surrounding matter from accreting into black hole)

$$\begin{array}{l} - \mbox{ Note also: } p,\rho,\sigma \mbox{ are inhomogeneous (pressure gradient prevents surrounding matter from accreting into black hole) \\ - \mbox{ Now consider 'extremal' case } M = Q: \ (\mbox{and def. } r = \frac{1}{\sqrt{k}} \tan \frac{\sqrt{k}\psi}{2}) \\ ds^2 = -\left[1 + M \frac{\sqrt{k}}{a \sin(\sqrt{k}\psi/2)}\right]^{-2} dt^2 \\ + a^2 \left[1 + M \frac{\sqrt{k}}{a \sin(\sqrt{k}\psi/2)}\right]^2 \left[d\psi^2 + \frac{\sin^2(\sqrt{k}\psi)}{k} \left(d\theta^2 + \sin^2\theta d\phi^2\right)\right], \\ F = d \left[\left(1 + M \frac{\sqrt{k}}{a \sin(\sqrt{k}\psi/2)}\right)^{-1} dt\right], \\ (\mbox{plus some expressions for } p, \rho, \sigma) \end{array}$$
- Note also: p, ρ, σ are inhomogeneous (pressure gradient prevents surrounding matter from accreting into black hole) - Now consider 'extremal' case M = Q: (and def. $r = \frac{1}{\sqrt{k}} \tan \frac{\sqrt{k\psi}}{2}$) $ds^{2} = -\left|1 + M\frac{\sqrt{k}}{a\,\sin(\sqrt{k}\,\psi/2)}\right| = dt^{2}$ $+a^{2}\left|1+M\frac{\sqrt{k}}{a\,\sin(\sqrt{k}\,\psi/2)}\right|^{2}\left|d\psi^{2}+\frac{\sin^{2}(\sqrt{k}\psi)}{k}\left(d\theta^{2}+\sin^{2}\theta d\phi^{2}\right)\right|,$ $F = d \left[\left(1 + M \frac{\sqrt{k}}{a \sin(\sqrt{k} \psi/2)} \right)^{-1} dt \right],$ (plus some expressions for p, ρ, σ)

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 $H = \frac{M\sqrt{k}}{\sin(\sqrt{k}\psi/2)}$ satisfies *conformal Laplace equation* on base space E³, S³ or H³, $\nabla^2 H = \frac{1}{8}RH$ (*R* = 6*k* scalar curvature)

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- A multi-centered solution is $H = \frac{1}{\sqrt{2}} \left[1 + k\vec{x}^2 \right]^{1/2} \sum_{I=1}^{I^*} \frac{Q_I}{|\vec{x} - \vec{x}_I|},$ obtained by using conformal invariance, $\tilde{\nabla}^2 \tilde{H} = \frac{1}{8} \tilde{R} \tilde{H}, \qquad \tilde{g}_{ij} = \Omega^2 g_{ij}, \qquad \tilde{H} = \Omega^{-1/2} H,$ $\tilde{g}_{ij} dx^i dx^j = \frac{4d\vec{x}^2}{\left[1 + k\vec{x}^2\right]^2}.$

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Consider single-centered asymptotically AdS case:
 (Is not Reissner-Nordström-AdS, but highly dynamical)

Metric:

$$ds^{2} = -\frac{g^{2}}{f^{2}}dt^{2} + a^{2}f^{2}\left(d\psi^{2} + \frac{\sin^{2}(\sqrt{k}\psi)}{k}d\Omega^{2}\right),$$

$$f = 1 + \frac{\sqrt{kM}}{a\sin(\sqrt{k\psi/2})} + k\frac{M^2 - Q^2}{4a^2\sin^2(\sqrt{k\psi/2})}, \qquad g = 1 - k\frac{M^2 - Q^2}{4a^2\sin^2(\sqrt{k\psi/2})}$$

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- Curvature singularities: $2a\sinh(\psi/2) = \sqrt{M^2 Q^2}$ For M = Q: $t = 0, t = l\pi$ or $\psi = 0$
- Trapping horizons (Hayward '93): Compute expansions of outgoing and ingoing radial null geodesics: $\theta_+ \equiv -2m^{(\mu}\bar{m}^{\nu)}\nabla_{\mu}l_{\nu}, \qquad \theta_- \equiv -2m^{(\mu}\bar{m}^{\nu)}\nabla_{\mu}n_{\nu}$

(l, m, n: Newman-Penrose null tetrad)

Marginal surfaces: Spacelike 2-surfaces on which $\theta_+ = 0$ ($\theta_- = 0$) Trapping horizons: Defined as closure of 3-surfaces foliated by marginal surfaces Marginal surfaces: Spacelike 2-surfaces on which $\theta_+ = 0$ ($\theta_- = 0$) Trapping horizons: Defined as closure of 3-surfaces foliated by marginal surfaces One finds the following:



Red: Curvature singularities (coincide w/ axes for M = Q) Blue: Trapping horizons (Green: Pair of radial null geodesics intersecting in $t = l\pi/2$)







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⇒ Only one point of the conformal boundary of AdS survives. ⇒ $\exists AdS/CFT$ interpretation in the usual sense?

- Black holes with unusual horizons:
 Noncompact manifolds w/ finite volume
 - Chiral excitations
 - violate reverse isoperimetric inequality \rightarrow 'superentropic'
 - can be generalized to higher dimensions and to presence of matter

Open questions:

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Open questions:

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Field theory interpretation?

Is this the end of the story?

Or can we have still more possibilities for the horizon geometry/topology in presence of a scalar potential?

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Why superposition principle? (Neither true nor fake susy)

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In such a scenario, the cosmological expansion would be driven by the scalars while rolling down their potential. (Cf. e.g. black holes constructed by Gibbons/Maeda in 0912.2809)